# Dynamic axial crushing of aluminium alloy 6063 - T6 circular tubes

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#### Abstract

An experimental investigation was carried out to study the behaviour of circular thinwalled aluminium alloy 6063T6 extrusions subjected to large axial impact loadings. The specimens, having an external diameter of 51 mm, were 1.5 mm thick, giving a 2R/H ratio of 33, approximately. Eighteen quasi-static and thirty-seven dynamic tests were performed and the primary variables were the specimen length ( $250 \le L \le 1200 \text{ mm}$ ), the impact mass ( $72 \le G \le 248 \text{ kg}$ ) and the initial velocity ( $3.33 \times 10^{-5} \le V_i \le 8.33 \text{ m/s}$ ) of the impact mass. The two latter variables were combined to give a constant input energy of 2.5 kJ in order to investigate the effect of inertia on the axial crushing of the aluminium alloy tubes without the contributory effect of material strain rate sensitivity.

The tensile stress-strain relations for the aluminium alloy 6063T6 of thickness 1.50 mm have been experimentally determined at room temperature (approximately  $20^{0}$ C) over a range of overall strain rates from  $5 \times 10^{-4}$ s<sup>-1</sup> to 118s<sup>-1</sup>, approximately. The yield and the ultimate tensile stresses of the material show a negligible dependency on strain rates, while the overall elongation exhibits a slight minimum at 0.03s<sup>-1</sup>, approximately. The corresponding large values of the Cowper-Symonds coefficients obtained using a least mean square fit, confirmed the strain rate insensitivity of the material.

Keywords: dynamic crushing, circular tubes, aluminium alloy 6063 T6, experiments, global bending, counterintuitive response

### Notation

 $\dot{\varepsilon}$  – overall strain rate, total  $\varepsilon$  divided by event time  $\dot{\varepsilon}_y$  – strain rate at  $\sigma_{0.2}$  divided by time to reach 0.2% yield stress  $\dot{\varepsilon}_u$  – strain rate of UTS  $\sigma_{0u}$ , divided by time to reach UTS  $\sigma$  – engineering stress  $\rho$  – Density  $\delta$  – crushed length After gl – gauge length after tensile test D, q – Cowper-Symonds coefficients

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 $\begin{array}{l} {\rm T-input\ energy}\\ E_h-{\rm hardening\ modulus}\\ {\rm elongation-(gl-after\ gl)/gl}\\ {\rm G-mass\ of\ striker}\\ {\rm gl-initial\ gauge\ length,\ 60mm}\\ {\rm H-thickness}\\ {\rm L-length\ of\ specimen}\\ P_m-{\rm mean\ load}\\ P_p-{\rm peak\ load}\\ {\rm R-mean\ radius\ of\ tube}\\ {\rm UTS-Ultimate\ Tensile\ Stress}\\ V_i-{\rm impact\ velocity}\\ {\rm W-width\ of\ tensile\ specimen}\\ \end{array}$ 

## 1 Introduction

The mechanics of dynamic plastic deformation of many ductile structures are influenced largely by two factors: the yield or flow stress of the material, which is dependent on the strain rate, and the deformation mode of the structure under dynamic loading which is different to the quasi-static mode on account of inertia forces [5]. The significance of these two factors, either acting separately or together, differs with different types and sizes of structures. For example, the deformation mode of an axially loaded tube might change when the initial tube length is increased or decreased with all of the remaining parameters unchanged. This transition length can be influenced by inertia forces.

Previous experimental studies on this phenomenon have examined the axial impact behaviour of mild steel [1], aluminium alloy [8] and stainless steel [7] tubes and a comparison between the behaviour of these three different materials has been made in Reference [9]. A counterintuitive behaviour has been observed in several experimental [8] and numerical [2,10,15,16] studies and this phenomenon is explored further in the current study for aluminium alloy 6063T6 circular tubes impacted axially.

In the present study, strain rate insensitive aluminium-magnesium-silicon alloy (Al-Mg-Si), grade 6063T6 circular tubes were crushed axially both quasi-statically and dynamically at a standard input energy of 2.5 kJ. The specimens, having an external diameter of 51 mm, were 1.5 mm thick, giving a 2R/H ratio of 33, approximately. This series of tests serves to (a) generate experimental data for the validation of numerical simulations; (b) study the effect of specimen length and inertia on the dynamic behaviour of Al-Mg-Si aluminium shells with a T6 temper, and (c) establish a transitional line separating the regions for progressive collapse and global buckling.

## 2 Material properties

The tube specimens were supplied in two batches, the first consisting of five tubes of 5 m lengths and the second of six tubes having 4 m lengths, from which the tensile specimens were machined. The nominal properties and chemical compositions of this alloy are shown in Table 1 [21]. The room temperature tensile properties of the material were determined from standard quasi-static and dynamic tensile tests. The variations in the thicknesses for the extruded components were between 1.48 mm and 1.55 mm (thickness =  $1.518 \text{ mm} \pm 2.3 \text{ per cent}$ , approximately), which is significant and may be an important factor to assess in any numerical modelling.

Aluminium Alloy	6063T6
$ ho,  g/cm^3$	2.7
$\sigma_{UTS}$ , MPa	240
$\sigma_Y$ , MPa	215
Elongation % (in 50mm)	12
E, Gpa	69
Al, Wt %	98.9
Cr	Max 0.1
Cu	Max 0.1
Fe	Max 0.35
Mg	0.45 - 0.9
Mn	Max 0.1
Si	0.2 - 0.6
Ti	Max 0.1
Zn	Max 0.1

Table 1: Material properties and composition of aluminium alloy 6063T6 [21].

## 2.1 Tensile tests

The tubes were cut in half across the cross-section and rolled flat. Tensile test specimens were then cut along the longitudinal direction of the tubing as 30 mm wide strips by 300 mm long.

The standard procedure for quasi-static tensile testing was conducted on an INSTRON 4204 tensile test machine. The head speed was set to 2mm/min giving an average overall strain rate,  $\dot{\varepsilon}_u$ , of 5 x 10<sup>-4</sup>s<sup>-1</sup>, approximately, for a gauge length of 60mm. The dynamic tensile tests were undertaken on a high-speed displacement controlled electro-servo hydraulic (ESH) machine at strain rates from 2 × 10<sup>-2</sup> to 118s<sup>-1</sup>. All the test specimens, except for two that were loaded quasi-statically, were strain gauged symmetrically on the front and back sides of the head and body. At least two specimens were examined at each test speed. The tensile tests results are

outlined in Table 2. The quasi-static 0.2% yield stress and UTS are 225MPa and 268MPa, respectively, and the rupture strain for a gauge length of 60mm is 8.9%. Figure 1 shows selected engineering stress-strain curves for the specimens at each test speed.

Specimen	W	H	gl	after	Overall	Test	Event	έu	έu	$\sigma_U$		$\sigma_u$	$E_{h}^{*}$	έ
	(mm)	(mm)	(mm)	gl	Elon-	Speed	time	5		(MPa)	0.1%	0.2%	(MPa)	
				(mm)	gation	(mm/s)	(s)							
					(strain)									
AA2	9.99	1.48	59.96	65.84	0.098	0.0333	195	0.000556		271	220	227	300	0.000503
AA3	9.98	1.51	59.96	65.26	0.088	0.0333	176	0.000556		271	220	227	300	0.000502
AA20	10.02	1.53	60.67	65.56	0.081	0.0333	150	0.000549		261	207	222	300	0.000537
AA1	10.01	1.53	60.15	65.05	0.081	2.000								
AA8	10.01	1.55	60.82	65.14	0.071	2.161	2.917	0.0029	0.0236	273	224	237	300	0.0244
AA13	9.97	1.48	59.30	64.54	0.088	2.0476	2.897	0.0029		275	223	231	300	0.0305
AA9	10.02	1.51	60.19	65.29	0.085	14.866	0.3288	0.0250	0.1804	268	217	232	300	0.2577
AA4	10.00	1.52	59.29	64.31	0.085	14.065	0.4468	0.0320	0.1771	278	219	237	300	0.1895
AA19	10.00	1.52	59.04	64.08	0.085	12.299	0.4950	0.0375	0.124	269	219	231	300	0.1725
AA17	10.00	1.52	59.96	65.09	0.086	164.2	0.0434	0.1772	1.7697	272	218	233	300	1.970
AA7	10.02	1.52	60.26	65.52	0.087	160.11	0.0462	0.24	2.0072	274	223	237	300	1.888
AA6	9.97	1.55	59.29	64.62	0.090	146.62	0.0500	0.17	1.2438	277	221	238	300	1.798
AA16	9.99	1.50	59.33	64.37	0.085	1502	0.0073	8.39	10.463	268	224	240	300	11.589
AA12	10.04	1.51	59.81	65.43	0.094	1500								
AA11	10.02	1.52	59.45	64.73	0.089	1338	0.0057	4.63	15.00	277	216	250	300	15.609
AA14	10.02	1.53	60.05	65.70	0.094	1434	0.0054	5.19	15.72	270	216	236	300	17.347
AA15	10.04	1.53	59.16	65.36	0.105	7179	0.0009	44.08	77.93	282	226	230	300	117.8
AA18	10.02	1.52	59.34	64.37	0.085	7341	0.0008	44.67	79.48	278	231	242	300	107.6

 $\ast$  slope of engineering stress-strain curve at 2% strain, approximately

#### Table 2: Tensile test results.

The behaviour of the 0.2% proof stress and UTS with respect to their respective strain rates are shown in Figures 2 and 3. As anticipated, this grade of aluminium alloy is virtually strain rate insensitive, which is consistent with many studies published previously [4, 6, 14, 22, 24]. Nonetheless an initial inspection of Figures 2 and 3 does reveal a slight increase in the 0.2% yield stress and UTS over the associated quasi-static values. A similar behaviour is observed for the proof stresses at strains of 1%, 2% and 5%. The corresponding increases in the flow stress at 0.2% proof stress and the UTS ( $\varepsilon > 0.05$ ) are both 5% when the overall strain rate was increased from 0.0005 to  $118s^{-1}$ . This behaviour may be compared with an increase of 12% in the UTS reported by Nicholas [22] for a similar grade of aluminium alloy, 6061T6, for strain rates up to  $600 \ s^{-1}$ . He revealed a negligible increase in the stress-strain curves up to approximately 10  $s^{-1}$  after which a greater degree of rate sensitivity at higher strain rates prevailed. Steidel and Makerov [14] found the UTS increased 5% for strain rates up to  $69s^{-1}$ , also for type 6061T6. It was concluded by Davies and Magee [6] that aluminium alloy 6061T6 had low a rate dependency for strain rates up to  $830s^{-1}$ .

The overall elongations of the specimens were between 7.1% and 10.5% for a gauge length of 60mm, as shown in Figure 4 as a function of the overall strain rate. In spite of the experimental scatter, the average elongation appears to decrease to a minimum at  $0.03s^{-1}$  and increases gradually to beyond the quasi-static values at  $118s^{-1}$ . This phenomenon has been observed to be more pronounced and distinct for stainless steel [7].



Figure 1: Engineering stress-strain curve at six different strain rates.



Figure 2: Variation of the 0.2% proof stress with strain rate.



Figure 3: Variation of the UTS with strain rate.



Figure 4: Variation of the total elongation with strain rate.

The data in Figures 2 and 3 are re-plotted in Figures 5 and 6, respectively, which give the Cowper-Symonds coefficients [13] at the two flow stresses using a least mean square fit. At yield,  $D = 9.390 \times 10^{10} s^{-1}$  and q = 9.55 and at the UTS,  $D = 4.7076 \times 10^{13} s^{-1}$  and q = 10.16. These values are much higher than the values of  $D = 6500 s^{-1}$  and q = 4 which are listed in Reference [13] and noted in Reference [4]. An earlier study [12] into the strain rate sensitive behaviour of aluminium alloy 6061T6 observed that the Cowper-Symonds equation with  $D = 1.288 \times 10^6 s^{-1}$  and q = 4 passed through the average of the widely scattered data of several experimental programs. The high values of D confirm the negligible strain rate sensitivity of

this material.

It should be noted that the average Vicker's hardness number of the axially crushed tubes is 78.3, while that for tensile test specimens is 97.5. The larger hardness numbers for the tensile test specimens is presumably due to the flattening process, which may have changed the mechanical properties of the aluminium alloy. If it is assumed that the Vicker's hardness number has a linear relationship with the UTS (a linear relationship with the Brinell hardness number has been used in Reference [23]), then the UTS of an untested tube, which has an average Vicker's hardness number of 80.6, would be  $2.814^1 \times 80.6 = 226.8$ MPa. This is about 15% smaller than the average UTS of 268MPa recorded in the tensile tests. Therefore, it raises questions on the accuracy of any numerical simulations which use constitutive relationships based on tensile specimens cut from flattened circular tubes.

## 3 Axial crushing of tubes

Eighteen quasi-static and thirty-seven dynamic tests were performed in the current study. Details of the tube lengths, impact masses and the corresponding impact velocities, which are calculated when assuming that a drop was frictionless, are listed in Table 3, while the quasistatic results are included in Table 2 of Reference [9]. The mean load,  $P_m$ , is defined as the total input energy, i.e. the initial kinetic energy, divided by the permanent axial crushing distance of a specimen, and was only calculated for specimens that collapse progressively. An input energy of 2.5KJ was adopted as a standard for all the dynamic tests in Table 3 and was chosen since it produced a reasonable number of complete wrinkles ( $\approx 6$ ) in a circular tube. The energy of 2.5KJ was imparted by dropping one of six different tup masses from the appropriate height.

Test ID	L (mm)	$\delta$ (mm)	G (kg)	$V_i (m/s)$	$\mathbf{P}_m$ (kN)	Failure Mode
DAASC42	700	68	72	8.33	36.8	A(5) bottom, slight bending
						$1/3  ext{ top}$
DAASC43	850	87	72	8.33	28.7	A(2) top, $A(4)$ bottom,
						sequence unknown, slight
						bending $1/3$ top with slight
						wrinkles
DAASC44	1005		72	8.33		no wrinkles on first impact,
						OB on secondary impact,
						bending wrinkles at $1/3$ bot-
						tom
DAASC45	1200		72	8.33		bending wrinkles along top
						1/3, top $1/4$ broke off

Table 3: Summary of dynamic axial crushing tests.

 $^{1}2.814$  is the average of all UTS values divided by the corresponding Vicker's hardness value from the tensile test.

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DAASC46	940		72	8.33		2 hinges, $1/3$ top and $1/3$
						bottom
DAASC47	750		72	8.33		OB $1/3$ top but bending
						wrinkles at $1/3$ bottom
DAASC16	900		102	7.00		A(5) bottom, OB 1/3 top, slight
						bending wrinkles
DAASC17	1000		102	7.00		A(1) top, OB above middle and
						1/3 top, slight tearing at wrinkle
DAASC18	800		102	7.00		A(1) top, OB $1/3$ top
DAASC19	750		102	7.00		OB $1/3$ top, severe tearing at
						hinge line
DAASC20	600		102	7.00		A(4.5) top, OB near top
DAASC36	450	70	103	6.97	35.7	A(5) top
DAASC37	500		103	6.97		OB above middle
DAASC38	550	80	103	6.97	31.3	A(4) top $A(1.5)$ bottom,
						slight bending at middle, se-
						quence unknown
DAASC39	580		103	6.97		OB above middle
DAASC40	400		103	6.97		A(1.5) top, OB above middle
DAASC41	350	94	103	6.97	26.6	A(7) top
DAASC55	400	83	117	6.54	30.1	A(2) D(2) top
DAASC56	500		117	6.54		A(4.5) top, OB middle
DAASC57	450	82	117	6.54	30.5	A(5.5) top, slight bending
						wrinkles at middle
DAASC58	550		117	6.54		OB above middle, severe
						tearing at hinge line
DAASC59	600		117	6.54		OB above middle
DAASC31	650		150	5.77		OB below middle, severe
						tearing at hinge line, 2nd
						hinge at 3 inches from bot-
						tom
DAASC32	600		150	5.77		OB middle, middle almost
						severed, 2nd hinge at 3
						inches from bottom, slight
						DPV at bottom
DAASC33	450		150	5.77		OB below middle
DAASC34	350	96	150	5.77	26.0	A(7) top, slight wrinkle at
						bottom
DAASC35	400		150	5.77		OB 1/3 top, severe tearijng
						at hinge line and all tube due
						to secondary impact*
DAASC60	500	79	149	5.79	31.6	A(6) top

Table 3: Summary of dynamic axial crushing tests.

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550	78	149	5.79	32.1	A(5.5) bottom, very slight
					bending wrinkles at $1/3$ top
491	85	193	5.09	29.4	A(3) top $A(1)$ $D(1)$ bottom,
					tearing at diamond wrinkle,
					slight bending wrinkles at
					middle and top
500		193	5.09		OB at $1/3 \text{ top}$ , severe crum-
					ble and tearing at hinge
550	84	193	5.09	29.8	A(2) D(1) top, tearing at di-
					amond wrinkle, slight bend-
					ing wrinkles
650		193	5.09		OB above middle, slight
					bending wrinkles near bot-
					tom
550	101	248	4.49	24.8	A(7) bottom
500		248	4.49		OB 1/3 top, tearing at hinge
					line
650		248	4.49		OB 1/3 top
500	100	248	4.49	25.0	A(7) top
	50         91           91         00           50         50           50         50           50         00           50         00           50         00	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	50 $78$ $149$ $5.79$ $91$ $85$ $193$ $5.09$ $00$ $193$ $5.09$ $00$ $193$ $5.09$ $50$ $84$ $193$ $5.09$ $50$ $84$ $193$ $5.09$ $50$ $101$ $248$ $4.49$ $00$ $248$ $4.49$ $50$ $248$ $4.49$ $00$ $100$ $248$ $4.49$	50 $78$ $149$ $5.79$ $32.1$ $91$ $85$ $193$ $5.09$ $29.4$ $00$ $193$ $5.09$ $29.4$ $00$ $193$ $5.09$ $29.4$ $50$ $84$ $193$ $5.09$ $29.8$ $50$ $84$ $193$ $5.09$ $29.8$ $50$ $101$ $248$ $4.49$ $24.8$ $00$ $248$ $4.49$ $24.8$ $00$ $100$ $248$ $4.49$ $25.0$

Table 3: Summary of dynamic axial crushing tests.

Small font size refers to specimens machined from the first batch of tubes, as with the quasi-statically tested specimens

\*secondary impact refers to the rebound of the tup mass

### 3.1 Experimental arrangement

The test arrangement which was employed in previous studies (eg. Ref. [7]) was used in the current study. Briefly, the quasi-static tests were performed on two compression machines: (a) Denison, with a maximum rating of 500kN for tubes shorter than 600mm long and (b) Dartec, with a maximum load of 250kN and a stroke of 100mm for tubes longer than 600mm. Both machines record the load-displacement histories at a constant pre-selected cross-head speed ranging from 2mm/min to 10mm/min, which was specified according to the specimen length. Each specimen was loaded while placed vertically on an anvil block and a test was halted as soon as it became unstable, or when the specimen was judged to have 'bottomed out'. One tube, SAASC17, was strain gauged at three positions to monitor the local strains near the top, bottom and the middle of the tube.

The impact tests were performed on a drop hammer rig (tup mass, G < 250kg, initial velocity,  $V_i < 14$  m/s). The specimens were loaded axially by a travelling mass while placed vertically on an anvil block. The velocity-time history was monitored by: (a) a Dantec Laser Doppler Anemometry (LDA) system and (b) a Kodak Ektapro high-speed camera with a film speed of



Figure 5: Determination of D and q for the 0.2% proof stress.



Figure 6: Determination of D and q for the UTS.

2000 frames per second (fps).

### 3.2 Collapse modes

The present tubes exhibit failure modes which are typical for these cross-sections and are similar to those for mild steel [1] and stainless steel [7] tubes. Figure 8 shows photographs of the final shapes of the test specimens for quasi-static (Figure 8(a)) and impact loads (Figure 8(b) -8(g)) with increasing pre-test lengths from left to right. Three principal modes of failure are identified: axisymmetric (A), also known as concertina, diamond mode (D) and overall bending (OB). The globally bent specimens tended to fail at the middle. Regular progressive collapse, on the other hand, can be initiated at either end with the formation of 7 (or 6 in one case) axisymmetric wrinkles before changing to a diamond mode with three vertices. Internal tearing always occurs on the wrinkle at a transition in a quasi-static test (Figure 9) and was revealed to have taken place on that particular wrinkle during the mode transition by stopping a quasistatic test prematurely. No tearing was observed in any subsequent wrinkles, nor when the tubes deformed only in an axisymetrical mode. The wrinkles initiated more frequently from the proximal end in the dynamic tests (13 out of 14 progressively collapsed tubes), but with no apparent dependence on the magnitude of the impact velocity. Slight internal tearing occurred at the transition wrinkle between axisymmetric and diamond behaviour in only two of the dynamic tests which responded in a progressive buckling mode.

Figure 7 shows three typical quasi-static load-displacement curves of tubes which crushed first in a concertina mode and then switched later to the diamond mode. It is evident that the pattern of behaviour is repeatable. The curves show that the twin peaks merge into a single peak which grows as the number of concertina wrinkles increase until a maximum value is reached, which then decreases immediately before the transition to a diamond mode occurs. The peaks then become smaller and less regular for further deformation.

A 400mm long tube, SAASC17, was strain gauged at 10mm from both ends and in the middle. It is evident from Figure 10(b) that the tube is uniformly compressed axially by 2.5mm, approximately, when the load reaches a peak value and the associated strain readings from the three gauges in Figure 10(a) exceed the plastic limit, i.e., 0.2% proof stress. Thus, the tube is in a state of uniform plastic compression before the development of any local buckling. The maximum recorded strain is 1.9%, approximately, which occurs at the distal end of a quasi-statically loaded tube where a wrinkle is partly (about one-half) formed.

It is noted that the failure modes of progressive collapse and global bending are random within the range  $300 \le L \le 440$ mm for the quasi-static results shown in Figure 8(a). In fact, Jensen et al. [11] observed a similar behaviour for aluminium alloy 6060T6 thin-walled square sections crushed axially. For a given local slenderness ratio, the static behaviour can change from global bending to progressive buckling and back to global bending as the axial length, L, is increased. However, an average value of the critical length for the present tests is 370mm, which turns out to be about 7 per cent larger than 345mm which is estimated from the classification



chart of Andrews et al. [3] for Ht 30 aluminium alloys with  $\sigma_{0.1} = 243$  MPa and  $\sigma_{0u} = 304$ MPa.

Figure 7: Load-displacement behaviour of three quasi-statically crushed tubes showing a transition between axisymmetric and diamond modes.

### 3.3 Inertia effects

It is well-known that material strain rate sensitivity and inertia effects are dominant features in the dynamic behaviour of Type II structures [5]. By choosing the almost strain rate insensitive aluminium alloy 6063T6 tubes, the effect of strain rate sensitivity can be largely discounted, so that the sole contribution of inertia on the failure mode can be analysed.

The experimental results in Table 3 are plotted in Figure 11 which shows the various failure modes plotted as a function of the initial impact velocity. One feature of this plot is the unexpected scatter of the failure modes for each test mass, which was not noted previously for axial impact tests on stainless steel [7] or mild steel [1] tubes, and which cannot be attributed to experimental error due to the general repeatability of the results. The scatter forms a transitional zone which reveals the sensitivity of the tube behaviour on the specimen length for a given impact velocity.

A transition line was drawn through the experimental data to separate the failure modes into two regions: progressive collapse and overall bending. Clearly, this transition line is different to the curves obtained for similar tests on stainless steel [7] and mild steel [1] tubes. The stability of the tubes increases up to an impact velocity of 5m/s, approximately, and declines for further increases in velocity up to 6.5m/s before improving again. The dip in stability with increase in impact velocity suggests the presence of an 'inverse' response or a counterintuitive phenomenon, as observed by Karagiozova and Alves [17] in the numerical modelling of axially loaded elasticplastic circular tubes which were made from a strain rate insensitive material. This anomalous



Figure 8: Final deformation profiles of the test specimens with increasing length from left to right.



Figure 9: Internal tearing of the wrinkle at a transition between axisymmetric (concertina) deformations and the diamond mode for specimen SAASC8 [9].

response has also been observed experimentally for aluminium alloy 6061T6 cylindrical tubes impacted axially in Reference [8] and has been explored numerically in References [10,15,17] and with simple models [16,18]. The absence of this counterintuitive phenomenon in the dynamic axial crushing of strain-rate sensitive tubes which are made of stainless steel [7] and mild steel [1] suggests that this behaviour may well be a characteristic response of aluminium alloy thin-walled sections which are strain rate insensitive.

The dynamic response of axially impacted tubes consist of two phases of motion; a uniform axial compression which is followed by local bending deformations [15, 16, 19]. Elastic and plastic stress wave propagation play a leading role in the dynamic response during the first phase of motion and the hardening modulus of the material controls the speed of any plastic waves [20]. It was shown in Reference [19] that the inertial resistance due to dynamic loadings having higher impact velocities may cause larger axial strains and stresses to develop during the axial compression phase before the subsequent shell buckling phase. Therefore, less energy is available for any subsequent local bending, which develops at higher stresses due to material strain hardening, thereby causing less deformation for a given amount of absorbed energy. The behaviour in Figure 12 is consistent with this idealisation since the total axial shortening of the specimens ( $\delta$ ) decreases with the impact velocity for a given impact energy. Thus, the mean load increases with the impact velocity (Figure 13) and decreases with the impact mass (Figure 14).

The idealised models in References [16, 18], were developed by recognising that a significant amount of impact energy could be absorbed in a wholly axial compression deformation mode before any local wrinkling (dynamic progressive buckling), or global bending, could occur. These idealised models have provided important insight into the complex behaviour of axially impacted elastic-plastic cylindrical shells. Currently, idealised models are being developed to explore the interaction between the different deformation modes rather than studying them largely in isolation as at present.



(a) Strain-time and load-time histories of the globally bent specimen SAAC17









Figure 11: Deformation map for aluminium alloy 6063T6 tubes for an impact energy of 2.5 kJ.



Figure 12: Crushed length against impact velocity.



Figure 14: Mean load against impact mass(T=2.5kJ-the impact mass in the quasi-static tests was taken as 1000kg).

## 3.4 Length effect

The total axial shortening of the tubes as a function of the specimen length is plotted in Figure 15 for an impact energy of 2.5kJ. The specimen length does not appear to influence significantly the crushed length for the six impact velocities examined, although there should be a tendency for  $\delta$  to decrease as L increases since more energy is absorbed elastically.



Figure 15: Crushed length against specimen length.

## 4 Conclusions

The material strain rate sensitive characteristics of aluminium alloy 6063T6 have been determined from dynamic tensile tests up to  $118 \text{ s}^{-1}$ . The results reveal that the yield stress and the UTS of aluminium alloy 6063T6 are essentially rate-insensitive within the investigated range of strain rates, which is consistent with previous results reported in the literature. The elongation, or rupture strain of the material, decreases and then increases with strain rate, showing a slight minimum at 0.03 s<sup>-1</sup>, approximately.

Experimental results have been reported for the axial compressive behaviour of thin-walled aluminium alloy 6063T6 circular tubes subjected to large axial impact loads. It transpires that the progressive buckling of the aluminium alloy thin walled sections have a tendency towards collapsing in an axisymmetrical mode for the first seven wrinkles before switching to a diamond mode with three-vertices. In the absence of material strain rate effects, it is evident that inertia effects influence the failure modes of the aluminium alloy shells for impact velocities up to 8.33m/s. The experimental results on the aluminium alloy tubes reveal the presence of an 'inverse', or counterintuitive, phenomenon, where the stability of a tube decreases with increase in impact velocity over a small range of velocities rather than continuing to increase. Finally, the initial length of a tube does not appear to have a distinct influence on the crushed length and, thus, the mean load.

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